

# T192

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# tl;dr

Given an array A containing N integers, where  $0 \leq A[i] < 3$ .

There are 3 operations:

1. L R x, change  $A[L..R] = x$
2. L R,  $A[i] = (A[i] + 1) \% 3$ ,  $L \leq i \leq R$
3. L R, find number of pairs(p, q) such that  $A[p..q]$  is colorful.

# Subtask 1

Just do what the problem states:

For operation 1: for loop change all elements.

For operation 2: for loop change all elements.

For operation 3: a nested for loop to calculate (p, q) that is colourful.

$O(Q * N^2)$

$O(Q * N^3)$  may pass too as there are only simple iteration.

## Subtask 2

Similar for subtask 1, we could see the bottleneck is calculating the no. of colourful pairs.

We could apply two-pointer technique to calculate.

$O(Q * N)$

# Subtask 3

Here there is only point update and range query.

We could come up with a segment tree solution.

Each node maintaining the no. of colourful strips in its segment, and the first and last occurrence of the three colours.

When we merge two nodes  $V$ ,  $U$  ( $V$  is on the left side and  $U$  on the right side), We try to calculate colourful strips that starts in  $V$  and ends at  $U$ . We could use the last occurrences of colours in  $V$  and first occurrences of colours in  $U$  to calculate.

$O(Q \log N)$

# Subtask 4

Here we have range update and range query.

So, we have to apply lazy propagation.

When we try to propagate from  $V$  (parent) to  $U$  (child), we need to handle some cases.

We first change  $U$  using the lazy value of  $V$ . Then,

If the lazy value of  $V$  is related to operation 1, then we know we could just simply change the lazy value of  $U$  to  $V$  and initialize node  $U$  information (like setting the  $ans = 0$ , first and last occurrence of that colour =  $(x, y)$ , other colour =  $-1$ ).

## Subtask 4

If the lazy value of V is related to operation 2:

if the lazy value of U is related to operation 2/ no lazy value:

change the lazy value  $(+ \text{ lazy value of V}) \% 3$ .

if the lazy value of U is related to operation 1:

we have to shift the colour of the lazy value  $(+ \text{ lazy value of V}) \% 3$

Notice that the related operation of lazy value of U is unchanged.

$O(Q \log N)$

# Subtask 5

The difference of subtask (3) 4 and 5 is the constant of your merging function of the segment tree node.

To pass subtask 5, your merging function should have constant  $\leq 3$  or applied some constant optimization in it.

You should carefully implement the segment tree, avoid using vector in the node.