

2016 MINI COMP 0

Tony Wong

2016-02-14

M1601 Valentine Day of Week

- Use computer clock to find out the Day of Week for 2000-02-14 (Monday)
- Use a for-loop to simulate years 2000 to N-1 (note that Feb 14 is before the leap day Feb 29)
 - +1 day for non-leap years ($366 \% 7 = 1$)
 - +2 days for leap years ($366 \% 7 = 2$)

M1602 Valentine Roses

- First, identify the position of the centre rose (3)
 - If the rose 3 is in the correct position, $A = 0$
Otherwise e.g. it is at (x, y) , swap (x, y) with $(3, 3)$ and $A = 1$
 - Just like Sample Test 1
- Count the number of “2”s around the perimeter, say B
 - That’s the number of swaps required to put the “2”s in the correct positions
- Overall answer = $A + B$
- Although here the size is fixed to be 5x5 (3 layers), think about:
 - What if there are N layers, or arbitrary size?
 - What if the pattern can be anything? (not just 1 around 2 around 3)

M1603 Valentine Kisses

- Process the messages one by one, maintaining a “state”
 - State 1: seen “>” followed by zero or more “3”s
 - State 0: otherwise (this is the default state)
- Whenever we see a “>”, switch to state 1 and initialize temp (the number of “3”s) = 0
- When we are in state 1 and see a “3”, **increase temp by 1**
- When we are in state 1 and see a “<”, **add temp to sum** and switch back to state 0
- When we are in state 1 and a character other than “3” or “<”, switch back to state 0

M1603 Valentine Kisses

		O	K	>	3	3	<	s	e	e	>	3	<
State	0	0	0	1	1	1	0	0	0	0	1	1	0
Temp	0	0	0	0	1	2	0	0	0	0	0	1	0
Sum	0	0	0	0	0	0	2	2	2	2	2	2	3

- Common Errors:
 - Failure to reset state to 0 after each message
 - Switch to switch 0 erroneously when encountering a “>” in state 1 (There should be 4 kisses in >>3333<<)

M1604 Valentine Sushi

- The first subtask can be simply solved by storing the data using a 2D (100x100) array as a list and processing the queries individually.
- The full solution requires some kind of $O(N \lg N)$ sorting (e.g. quick sort / merge sort)
- Note that for $R < L$, the query has to split into two parts:
 - $1 \dots R, L \dots N$
 - (actual answer is OR of the two)

M1604 Valentine Sushi

- Although not required, you can store their favourite dishes in a single array **A** of size $\sum D_i$ by “flattening”.
- For the sample picture, the array would be:
- With these arrays, the queries become:
Does number **X** exist in the subarray
 - $A[SS[L]] .. A[SE[R] - 1]$ for $L \leq R$
 - $A[SS[L]] .. A[SE[N] - 1]$ or $A[SS[1]] .. A[SE[R] - 1]$ for $L > R$

0	1	2	3	4	5	6	7	8
1	3	2	1	1	2	3	4	4

SS: Seat Start (included)	SE: Seat End (included)
0	2
2	3
3	3
3	4
4	6
6	7
7	8
8	9


M1604 Valentine Sushi

- After splitting, sort the queries by L then R (Keep the query IDs)
- Maintain M lists, one for each color
 - Initially they are all empty
 - These lists are for storing which queries are “active”
 - Each element is a pair of integers: R and ID
- Go through Seats $i = 1 \dots N$ one by one
 - Insert queries with $L = i$ into the lists (the queries become active)
 - For each color j in seat i : go through list j and clear the list at the end
 - If the query should be expired, i.e. $i > R$, just ignore it
 - Otherwise, the answer for query ID is Yes
- Overall complexity: $O(N + M + \sum D_i + Q \lg Q)$

M1604 Valentine Sushi

- Alternative solution using binary search tree (set)
- There will be M sets (one for each dish)
- Insert all the seat numbers for Dish i into set i
- For each query, determine whether there exist a number in $L .. R$ / $L .. N$ or $1 .. R$ in set X
 $s[x].lower_bound(l) \neq s[x].upper_bound(r)$
- Overall complexity: $O(N + M + \sum D_i + Q \lg N)$

M1605 Valentine Gift Box

- The second approach is to identify the pattern: 
- If processed from top to bottom, left to right, seeing this pattern would mean it is the top-left corner of a box
- Obtain the width w , height h of the empty space by looking for `##`
 - You will see `#.` until the ribbon
- Area of the box = $(2w + 1) \times (2h + 1)$
- Finally, you need to erase the box by replacing the whole area with some other character to avoid duplicate processing

