



**Secret message**



# Problem description

A string is transformed to another string by Burrow-Wheeler Transform

Final string --> initial string

Full :  $N \leq 2 \cdot 10^5$



# 15% solution

- only 'A', 'B' and '#',  $N \leq 10$
- Enumeration
- $O(2^N)$



# Observation

- what is the first letter in the original string?
- Do we know the characters in first column?
- Relation between first character and last character?



# 20% solution

- $N \leq 27$ , all characters are unique
- sort the characters given to obtain first column
- start from the row that contains '#' in last column
- Let the character be  $x$ , move on to the next row that contains  $x$  in last column, and push  $x$  into answer string, repeat until the string is full
- $O(N^2)$  to  $O(N)$  depends on how you implement it



# Observation

- Problem arises if characters are not unique
- Seems we have no clue about where the next row is



# Observation

- For the character ranked  $x$  (among the same character) in the first column, the character it represents in the last column also ranks  $x$  (among the same character)



# 100% solution

- $N \leq 2 \cdot 10^5$
- sort the characters given to obtain first column
- start from the row that contains '#' in last column
- Let the character be x, move on to the next row that x **represents in the last column**, and push x into answer string, repeat until the string is full
- $O(N^2)$  to  $O(N)$  depends on how you implement it





# Implementation stuff

How to sort characters in the original string in  $O(N)$ ?

Bubble sort  $O(N^2)$

Merge sort  $O(N \lg N)$

Count sort  $O(N + E)$   $E$  = number of characters available

How do we get the next row in  $O(1)$ ?

2D array