# 2021 Team Formation Test

# Task Overview

ID	Name	Time Limit	Memory Limit	Subtasks
T211	Snow Way	1.000 s	1024 MB	5 + 23 + 26 + 34 + 12
T212	Food Kangaroo	2.000 s	1024 MB	6 + 11 + 15 + 24 + 22 + 22
T213	Game Developer	2.000 s	1024 MB	16 + 4 + 21 + 6 + 14 + 34 + 5
T214	Re:Zero	1.000 s	1024 MB	100

#### Notice:

Unless otherwise specified, inputs and outputs shall follow the format below:

- One space between a number and another number or character in the same line.
- No space between characters in the same line.
- Each string shall be placed in its own separate line.
- Outputs will be automatically fixed as follows: Trailing spaces in each line will be removed and an end-of-line character will be added to the end of the output if not present. All other format errors will not be fixed.

C++ programmers should be aware that using C++ streams (cin / cout) may lead to I/O bottlenecks and substantially lower performance.

For some problems 64-bit integers may be required. In C++ the data type is long long and its token for scanf/printf is %11d.

All tasks are divided into subtasks. Unless otherwise specified, you need to pass all test cases in a subtask to get points.

#### T211 - SNOW WAY

Alice and Bob are training for their sledding competition, in which they slide down a snowy slope following the guidance of various signposts.

Consider the snowy slope as a triangular grid of size N, which has i cells on the i-th row:  $(i,1),(i,2),\ldots,(i,i)$ . Initially, all the cells are empty with no signposts placed on them. Starting at (1,1), Alice wants to reach cell (N,X), while Bob wants to reach cell (N,Y)  $(X \leq Y)$ , but they cannot do so unless guided by the signposts appropriately.

There are two types of signpost: type-A signposts and type-B signposts. Each signpost can be placed in exactly one cell (except cells in row N) to mark the sledding direction. The type of the signpost would affect how Alice and Bob's moves:

- Suppose Alice is at cell (i, j),
  - O If the cell is unmarked, Alice stops there.
  - $\circ$  If the cell is marked with a type-A signpost, Alice moves to (i+1,j).
  - $\circ$  If the cell is marked with a type-B signpost, Alice moves to (i+1, j+1).
- Suppose Bob is at cell (i, j),
  - If the cell is unmarked, Bob stops there.
  - $\circ$  If the cell is marked with a type-A signpost, Bob moves to (i+1, j+1).
  - $\circ$  If the cell is marked with a type-B signpost, Bob moves to (i+1,j).

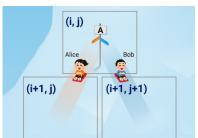


Figure 2a: Movements when a type-A signpost is placed.

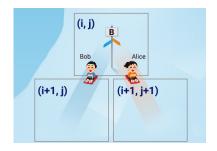


Figure 2b: Movements when a type-B signpost is placed.

You have A type-A signposts and B type-B signposts. You want to place these signposts on the grid, so that Alice and Bob can both reach their destinations. You should not place more than one signpost in a single cell to avoid confusing them. Again, signposts cannot be placed at row N for obvious safety reasons (they will fall out of the grid).

Your task is to either find a way to place the signposts, or determine that it is impossible for both Alice and Bob to reach their destinations. If there are more than one way, output any one of them. Please note that there is no need to use all the signposts and also no need to ensure that Alice or Bob can utilize a signpost.

#### **INPUT**

The first line contains three integers, N, A, and B. The second line contains two integers, X and Y.

Time Limit:  $1.000\ s$  / Memory Limit:  $1024\ MB$ 

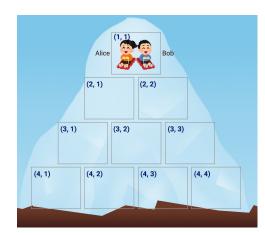


Figure 1: A triangular grid of size 4.

# **OUTPUT**

If there is no solution, output [NO] in the first and only line.

Otherwise, output [YES] in the first line.

Then, on the next line, output an integer  $T_A$  ( $0 \le T_A \le A$ ), the number of type-A signposts used.  $T_A$  lines should follow, each line containing two integers, the row and column of a type-A signpost.

On the next line, output an integer  $T_B$  ( $0 \le T_B \le B$ ), the number of type-B signposts used.  $T_B$  lines should follow, each line containing two integers, the row and column of a type-B signpost.

The signposts can be output in any order. You score zero if you place more than one signpost on the same cell.

# SAMPLE TESTS

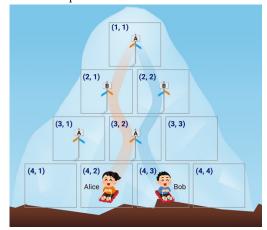
	Input	Output
1	3 2 2 2 2	YES 2
		2 1 2 2
		1
	_	1 1
	(2, 1)	(2, 2) À
	(3, 1) (3, 2) Bob	(3, 3) Alice

Alice's path:  $(1,1) \rightarrow (2,2) \rightarrow (3,2)$ Bob's path:  $(1,1) \rightarrow (2,1) \rightarrow (3,2)$ Note that not all signposts were used.



2	4 8 8	YES
	2 3	3
		1 1
		3 2
		3 1
		2
		2 2
		2 1

One of the possible solutions is as follows:



# **SUBTASKS**

For all cases:

$$2 \leq N \leq 10^5$$

$$0 \leq A, B \leq 2 \times 10^5$$

$$1 \leq X \leq Y \leq N$$

Points Constraints

$$2 \qquad 23 \qquad A=B=2\times N \\ 2\leq N\leq 30$$

3 
$$26 2 \le N \le 30$$

4 
$$34 \quad X < Y$$

5 12 No additional constraints

Time Limit: 2.000 s / Memory Limit: 1024 MB

## T212 - FOOD KANGAROO

rider to earn some money.

Recently, everyone in Byteland are so lazy that they cannot be bothered cooking or going out for a meal. A food delivery platform "Food Kangaroo" was founded to collect food orders. Delivery riders can choose to take delivery orders and carry lunch boxes from restaurants to the destinations. After a hard-fought efforts to pass the driving test, Bob decides to be a delivery

In Byteland, there are N cities. Cities are numbered from 1 through N. There are  $(H_F + H_T)$  highways,  $H_F$  of them are free while  $H_T$  of them are toll. Each highway connects a pair of distinct cities. No two highways connect the same pair of cities. Bob needs to pay toll every time he drives through a toll highway. Bob can drive on any highway in both directions.

There are D delivery orders posted, and each of them can be taken infinitely many times. The  $k^{th}$  order requires a lunch box delivery from city  $X_k$  to city  $Y_k$ . It is guaranteed that cities  $X_k$  and  $Y_k$  are connected through some highways and  $X_k \neq Y_k$ . Delivery rider can only take the order when he is at city  $X_k$ . When he takes the order, he carries a lunch box from city  $X_k$  to city  $Y_k$ . When he arrives city  $Y_k$ , the lunch box is considered as delivered and he receives a reward of  $R_k$  Bytecoins.

Bob starts his job as a delivery rider from city 1 and ends his duty in any city he wants. He uses a smart card called "Byteca" to pay tolls and receive rewards. The balance of "Byteca" ranges from negative infinity to positive infinity so tolls can still be paid even when the balance is less than the toll. Specifically, Bob can still pay tolls when the balance is negative.

Bob can drive along the roads to take orders and carry lunch boxes. Bob does not have any time limit to deliver orders and he can take infinitely many orders. However, at any give moment, he could carry at most one lunch box.

As a friend of Bob, please find out if he is able to earn infinitely many Bytecoins or the maximum Bytecoins he can earn if he takes and delivers orders optimally.

#### **INPUT**

The first line contains four integers:  $N, H_F, H_T$  and D.

The  $i^{th}$  of the next  $H_F$  lines, each contains two integers  $u_i$  and  $v_i$ : the  $i^{th}$  free highway connects city  $u_i$  and  $v_i$ .

The  $j^{th}$  of the next  $H_T$  lines, each contains three integers  $u_j$ ,  $v_j$  and  $t_j$ : the  $j^{th}$  toll highway connects city  $u_j$  and  $v_j$ , and its toll is  $t_j$  Bytecoins.

Each highway connects a pair of distinct cities. No two highways connect the same pair of cities.

The  $k^{th}$  of the next D lines, each contains three integers  $X_k$ ,  $Y_k$  and  $R_k$ : the  $k^{th}$  delivery order requires delivery from city  $X_k$  to  $Y_k$ , and its reward is  $R_k$  Bytecoins.

It is possible that multiple deliver orders share the same  $X_k$  and/or  $Y_k$ .

#### **OUTPUT**

If there is a way to earn infinitely many Bytecoins, output [YES] on the first and only line.

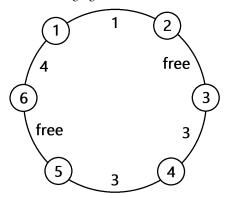
Otherwise, on the first line, output NO. On the second line, output an integer, the maximum Bytecoins Bob can earn.



# SAMPLE TESTS

	Input	Output
1	6 2 4 1	NO
	2 3	1
	6 5	
	1 2 1	
	3 4 3	
	4 5 3	
	6 1 4	
	2 5 7	

The following figure shows the roads connecting the cities:



Bob can travel in the following way:

 $1 \rightarrow 2 (\text{pick up order 1}) \rightarrow 1 \rightarrow 6 \rightarrow 5 (\text{deliver order 1})$ 

6 2 4 1	NO
2 3	1234567
6 5	
1 2 1	
3 4 3	
4 5 3	
6 1 4	
2 5 7	
	2 3 6 5 1 2 1 3 4 3 4 5 3 6 1 4

This output scores 30% in subtasks excluding Subtask 5.

3	6 2	4 3	YES
5		т 3	ILS
	2 3		
	6 5		
	1 2	1	
	3 4	3	
	4 5	3	
	6 1	4	
	2 5	7	
	6 3		
	5 6	3	

Bob can travel in the following way:

 $\begin{array}{l} 1 \rightarrow 2 (\text{pick up order 1}) \rightarrow 3 \rightarrow 4 \rightarrow 5 (\text{deliver order 1, pick up order 3}) \rightarrow 6 (\text{deliver order 3, pick up order 2}) \\ \rightarrow 1 \rightarrow 2 \rightarrow 3 (\text{deliver order 2}) \rightarrow 2 (\text{pick up order 1}) \rightarrow 3 \rightarrow 4 \rightarrow 5 (\text{deliver order 1, pick up order 3}) \rightarrow \dots \end{array}$ 

4	7 3	3 5 3	NO
	2 1		2
	3 4		
	5 6		
	6 7		
	2 4		
	5 7	' 3	
		3 4	
	2 3		
	3 2		
	7 5		
	1 3	3 5	

## **SUBTASKS**

For all cases:

$$2 \leq N \leq 2 \times 10^5$$

$$0 \leq H_F, D \leq 2 imes 10^5$$

$$0 \le H_T \le 500$$

$$1 \le t_j \le 10^9$$
 (for all  $1 \le j \le H_T$ )

$$1 \le R_k \le 10^9$$
 (for all  $1 \le k \le D$ )

#### Points

Constraints

1 6 
$$H_T = 0$$

$$2 11 D = 1$$

$$3$$
 15  $2 \le N \le 50$   $H_F = 0$   $0 \le D \le 10$   $0 \le H_T \le 50$ 

4 24 
$$H_F = 0$$

5 22 There is no way to earn infinitely many Bytecoins.

6 22 No additional constraints.

#### **SCORING**

In subtasks except Subtask 5, you can obtain a partial score. For each subtask (except Subtask 5):

- You score 100% if your output is correct in all test cases within the subtask; otherwise
- You score 30% if the first line of your output is correct in all test cases within the subtask; otherwise
- You score 0.

Note that your program shall still fulfill the output format specified (i.e. output an integer on the second line in  $\boxed{NO}$  cases) even if it is attempted for partial score.

### T213 - GAME DEVELOPER

Time Limit: 2.000 s / Memory Limit: 1024 MB

Bob is a game developer and he is making a game for Alice, his girlfriend, as Valentine Day's gift. He knows that Alice likes fighter games, so he wants to make a game with N+1 stages, the stage are numbered from 0 to N.

At the beginning, only stage 0 is unlocked. For each stage  $1 \le i \le N$ , if you beat stage  $P_i$   $(0 \le P_i \le i - 1)$ , then stage i is unlocked.

Bob, wanting to make Alice happy, has made N presents, numbered from 1 to N, and the j-th present has value  $V_j$ . He now has to assign a present to every stage except stage 0. Formally, Bob shall assign present  $m_i$  to stage i, where  $m_{1..N}$  is a permutation of 1..N. Denote  $R_i$  as the value of the present assigned for stage i, we have  $R_i = V_{m_i}$ .

He wants to assign the presents in such a way that for all  $1 \le i \le N$ ,  $R_{P_i} \le R_i$ , that is the value of present assigned to stage i is larger than or equal to the value of present of the stage that unlocks stage i. For simplicity, we treat  $R_0 = 0$  here as no present is assigned to stage 0.

Bob introduces this game to Alice. Alice observes that playing the game in the order of stage 1, 2, ..., N is always possible as  $P_i \le i - 1$ , so Alice has decided to play the game in this order.

After Bob knows the order of stages that Alice will play in, he wants to maximize the value of presents Alice will get early so she will be happier, so he wants to assign the presents in a way that obtains the lexicographically greatest sequence of  $R_{1..N}$  while satisfying the requirements above.

A sequence  $x_1, x_2, \ldots, x_N$  is lexicographically greater than the sequence  $y_1, y_2, \ldots, y_N$  if there exists  $i \ (1 \le i \le N)$  such that  $x_i > y_i$  and for all  $j \ (1 \le j < i)$ ,  $x_j = y_j$ .

#### **INPUT**

The first line contains an integer N.

The second line contains N integers, the j-th integer is  $V_j$ .

The third line contains N integers, the i-th integer is  $P_i$ .

#### **OUTPUT**

Output N space-separated integers on one line, the lexicographically greatest sequence of  $R_{1..N}$  that satisfies all the requirements. The i-th integer is  $R_i$ . It can be proven that there always exist such  $R_{1..N}$  that satisfies all the requirements.

# SAMPLE TESTS

Output

 4
 6 7 8 9

 0 1 1 2
 6 8 7 9

 $\{6,7,8,9\}, \{6,7,9,8\}, \{6,8,7,9\}$  satisfy the requirement  $R_{P_i} \leq R_i$  The lexicographically greatest one is  $\{6,8,7,9\}$ .

2 4 5 6 6 6 6 6 7 8 9 1 1

 $\{5, 5, 6, 6\}, \{5, 6, 5, 6\}, \{5, 6, 6, 5\}$  satisfy the requirement  $R_{P_i} \leq R_i$  The lexicographically greatest one is  $\{5, 6, 6, 5\}$ .

# **SUBTASKS**

For all cases:

 $1 \le N \le 10^6$ 

 $1 \leq V_i \leq 10^9$ 

 $0 \leq P_i \leq i-1$ , for all  $1 \leq i \leq N$ 

#### Points Constraints

 $\begin{array}{ccc} \textbf{1} & 16 & 1 \leq N \leq 2 \cdot 10^5 \\ & V_i \text{ are distinct} \end{array}$ 

 $2 4 1 \le N \le 8$ 

3  $21 \quad 1 \le N \le 200$ 

4 6  $1 \le N \le 1000$ 

5  $14 \quad 1 \le N \le 5000$ 

6  $34 1 \le N \le 2 \cdot 10^5$ 

7 5 No additional constraints

Time Limit: 1.000 s / Memory Limit: 1024 MB

#### T214 - RE:ZERO

In the anime《Re:Zero – Starting Life in Another World》(Re:ゼロから始める異世界生活), the protagonist -- Subaru finds

himself transported to another world on his way home from the convenience store. Upon his arrival in the new world, Subaru realizes that he acquired a new ability "Return by Death" that allows him to go back to the time when he died while still retaining his memories of what he has experienced. In other words, this ability allows him to "foresee" the future in exchange for his death.

A villain, Elsa wants to kill Subaru. Therefore, she has summoned N monsters at Day 0 which are labelled 0 to N-1. The monsters will move around the town and destroy the city unless Subaru surrenders to Elsa. The city can be viewed as a number line and the origin of the city is point 0. Each monster's starting position is an integer value that the absolute value shows the unit distance between the monster and the origin. If the value is negative, then the monster is on the left side of the origin. If the value is positive, then the monster is on the right side of the origin. Note that the starting positions might not be distinct as they may attack the city as a group.

The monster i's movement can be described by integers  $X_i$  and  $T_i$ , where the monster would move  $|X_i|$  units every  $T_i$ -th day (i.e. if  $T_i = 7$ , then the monster would move at the beginning of Day 7, 14, 21...). If  $X_i$  is positive, the monster would move to the right while if  $X_i$  is negative, the monster would move to the left. Unfortunately, all starting positions,  $X_i$  and  $T_i$  of the monsters are unknown to Subaru.

Subaru has found out that when he surrenders to Elsa at Day D, Elsa, without knowing Subaru has the ability "Return by Death", would expose the positions of all the monsters at the end of Day D before killing Subaru just to tease him. And Subaru will return to Day 0 as it activates his ability. In short, if Subaru surrenders at Day D, he can get the positions of all monsters at the end of Day D and returns to Day 0 again.

Defeating Elsa is easy, but Subaru doesn't want anyone in the city to be injured. So he has to gather the values of all  $X_i$  and  $T_i$  in order to schedule the evacuation plan for the citizens. As you can imagine, the feeling of dying is unbearable for anyone. Being a friend of Subaru, please help him to find all  $X_i$  and  $T_i$  with Subaru dying as few times as possible.

#### **IMPLEMENTATION DETAILS**

You should implement the following procedure:

std::vector<std::pair<int, int>> analyze monsters(int N)

- *N*: the number of monsters.
- This procedure will be called exactly once by the grader.
- It should return an array of pairs P of length N, indicating the information of each monster's movement, with P[i]. first representing monster i's  $X_i$  and P[i]. second representing  $T_i$ .

The above procedure can make calls to the following procedure:

std::vector<long long> surrender(long long D)

- *D*: the Day that Subaru surrenders to Elsa.
- D is at least 0 and at most  $10^{15}$ .
- This procedure will return an array S of length N, where S[i] represents the position of the monster i at the end of day D.

Notice: your submission must not perform any of the following actions, which result in an unspecified grading verdict:

- read from the standard input, write to the standard output, or interact with any other file,
- call exit()

Note that the grader is not adaptive. The labels, starting positions,  $X_i$  and  $T_i$  of the N monsters are fixed before the start of the interaction.

## SAMPLE RUN

Suppose N=2, monster 0 has a starting position of 0 and moves 2 units towards right every 3rd day, while monster 1 has a starting position of 2 and moves 3 units towards left every 4th day. The procedure analyze\_monsters is called in the following way:

Explanation

analyze monsters(2)

Function Call

This procedure may call the followings in such order:

Returns

surrender(5)	[2, -1]	Subaru surrenders at Day 5.
		The position of the monsters at the end of Day 5 are 2 and -1.
surrender(6)	[4, -1]	Subaru surrenders at Day 6.
	_ , _	The position of the monsters at the end of Day 6 are 4 and -1.
surrender(2)	[0, 2]	Subaru surrenders at Day 2.
, ,	_ , _	The position of the monsters at the end of Day 2 are 0 and 2.
surrender(4)	[2, -1]	Subaru surrenders at Day 4.
	_ , _	The position of the monsters at the end of Day 4 are 2 and -1.
surrender(3)	[2, 2]	Subaru surrenders at Day 3.
		The position of the monsters at the end of Day 3 are 2 and 2.

At this point, there is sufficient information to conclude that  $X_0 = 2$ ,  $T_0 = 3$ ,  $X_1 = -3$  and  $T_1 = 4$ . As such, the analyze\_monsters procedure should return [(2, 3), (-3, 4)].

#### **CONSTRAINTS**

•  $1 \le N \le 1000$ 

For all  $0 \le i \le N-1$ :

- ullet  $-10^{18} \leq$  monster *i*'s starting position  $\leq 10^{18}$
- $-1000 \le X_i \le 1000$
- $\bullet$   $X_i \neq 0$
- $1 \le T_i \le 100$

## **SCORING**

If in any of the test cases, the calls to the procedure [surrender] do not conform to the rules mentioned above, or the return value of  $[analyze\_monsters]$  is incorrect, the score of your solution will be 0. Otherwise, let W be the maximum number of calls to the procedure [surrender] among all test cases. Then, the score will be calculated according to the following table:

Condition	Score	
130 < W	0	
$8 \leq W \leq 130$	$72-6.5\cdot\sqrt{W-7.5}$	
$4 \leq W \leq 7$	$100-6.9\cdot(W-3)$	
$W \leq 3$	100	

Your score on this task is the lowest score you get among all test cases.

# SAMPLE GRADER

In order to test your program, you may download the sample grader files.

Language	Source Code Filename	Compilation Command	Execution Command
C++17	rezero.cpp	./compile_cpp.sh	./rezero

Please be advised that although the sample grader is intended to simulate the judging system, it is NOT the real judging system and might behave differently.

When testing your programs with the sample grader, your input should match the format and constraints from the task statement. Otherwise, unspecified behaviors may occur.

The sample grader reads the input in the following format:

- line 1: *N*
- next N lines:  $Position_i X_i T_i$ , where
  - $\circ$  *Position*<sub>i</sub> is the starting position of monster i.
  - $\circ$   $X_i$  and  $T_i$  are the values of monster i mentioned above.

The sample grader prints your answers in the following format:

- ullet first N lines:  $X_i$   $T_i$  as reported by analyze\_monsters
- line N+1: the number of calls to surrender.