

Assume that all variables without declaration shown in the following program segments have already been declared properly. Integers in problem statements are 32-bit signed variables (**Pascal**: `longint`, **C**: `int`). Assume all the programs are compiled properly without using any compiler flag (except the `-o` option in C).

	Format	# Questions	Total Marks
Section A1	True or False	5	5
Section A2	Multiple Choice	20	20
Section B	Fill-in-the-blanks	6 (A-K)	22
Total			47

Section A1 (5 marks)

For each question, determine whether the statement is true or false, then put down **T** or **F** in the corresponding space on the answer sheet. One mark for each correct answer. No marks will be deducted for wrong answers

- The performance of cloud computing is reduced in a sunny day without cloud.
- Overflow may occur when you add two negative integers.
- Given n is an integer, **Pascal**: $n \text{ div } 2$, **C**: $n/2$ is always less than or equal to $n/2.0$
- There exists N such that there are more even numbers than odd numbers in the first N numbers in the Fibonacci sequence 1, 1, 2, 3, 5, 8, 13, ...
- `break;` and `continue;` are both valid statements in all while loop, do-while loop and for loops.

Section A2 (20 marks)

For each question, choose the most appropriate answer and write the letter (A, B, C or D) in the corresponding space on the answer sheet. One mark for each correct answer. No marks will be deducted for wrong answers.

6. Tic-tac-toe is a 2-player game. Each player takes turn to draw 'O' or 'X' onto a 3x3 grid. The first player chooses an empty cell to draw a 'O', then the second player chooses another empty grid cell to draw a 'X', and so on, until all cells are filled. A player wins if he can draw 3 same symbols ('O' or 'X') along any horizontal, vertical or diagonal line. If both players fail to do so, the game ends in a draw.

Given that both players do not want to lose. Which of the following situation(s) will turn out to end in a draw?

i.

	X	O

ii.

X		
O		

- A. i only
 B. ii only
 C. i and ii
 D. None of the above

7. A stands in front of B, B stands in front of C, C stands in front of D.

The distance between A and C is less than or equal to 5 meters.

The distance between B and D is less than or equal to 9 meters.

The distance between B and C is greater than or equal to 3 meters.

What is the greatest possible distance between A and D?

- A. 7
 B. 8
 C. 11
 D. 17

8. Given x and y are non-negative integers, what is the largest integer that cannot be obtained from $3x+7y$?

- A. 5
 B. 7
 C. 11
 D. 13

9. What is the output of the following program?

Pascal Version

```
begin
  write('H');//write('K');
  //write('O'); write('I');
  write('2');//write('0');
  //write('1'); write('3');
end.
```

- A. H2
- B. HI23
- C. HK20
- D. HKOI2013

C Version

```
#include <stdio.h>
int main(){
  printf("H");//printf("K");
  //printf("O"); printf("I");
  printf("2");//printf("0");
  //printf("1"); printf("3");
  return 0;
}
```

10. What is the return value of function $f()$?

Pascal Version

```
function f:longint;
var i,k:longint;
begin
  k := 2;
  for i:=1 to 2013 do
    if (i mod k = 0) then
      k := k*2;
  f := k;
end;
```

- A. 1024
- B. 2048
- C. 32768
- D. 65536

C Version

```
int f() {
  int i, k = 2;
  for (i=1; i<=2013; ++i)
    if (i % k == 0)
      k = k*2;
  return k;
}
```

11. What is the output of the following program?

Pascal Version

```
var
  a:array[0..7] of longint =
    (4,7,1,6,2,8,3,5);
  x,ans,i,j,t:longint;
begin
  x:=4;
  for i:=0 to x-1 do
    for j:=1 to 7-i do
      begin
        if (a[j-1] > a[j]) then
          begin
            t := a[j-1];
            a[j-1] := a[j];
            a[j] := t;
          end;
        ans:=a[j];
      end;
    write(ans);
  end.
```

C Version

```
#include <stdio.h>

int a[8] = {4,7,1,6,2,8,3,5};
int x=4, ans=-1, i, j, t;

int main() {
  for (i=0; i<x; ++i)
    for (j=1; j<8-i; ++j) {
      if (a[j-1] > a[j]) {
        t = a[j-1];
        a[j-1] = a[j];
        a[j] = t;
      }
      ans = a[j];
    }
  printf("%d", ans);
  return 0;
}
```

- A. 3
- B. 4
- C. 5
- D. 6

12. X, Y and Z are specialized at making wineX, wineY and wineZ respectively. The three persons are smart and they have a way to fairly trade their wine among each other. The total value of wine received by one is equal to the value he gave away.

Suppose X kept half of wineX and gave one-fourth of wineX to Y and one-fourth to Z.

Y divided wineY evenly among the three persons, one-third going to each other.

Z gave half of wineZ to X and divided the other half wineZ evenly between Y and himself.

The result is summarized in the following table:

	wineX	wineY	wineZ
X	1/2	1/3	1/2
Y	1/4	1/3	1/4
Z	1/4	1/3	1/4

If wineZ is worth 3 thousand dollars. What are the values (in thousand dollars) of wineX and wineY respectively?

- A. wineX: 3 wineY: 4
- B. wineX: 4 wineY: 3
- C. wineX: 5 wineY: 3
- D. wineX: 6 wineY: 3

13. There are 8 booleans, named A, B, ..., H.

- | | |
|--------------------------------|--------------------------------|
| A and E have the same value. | A and B have different values. |
| D and B have different values. | C and D have the same value. |
| D and G have different values. | F and D have different values. |
| F and G have the same value. | |

Which of the following **MUST** be correct?

- A. A and H have the same value.
- B. B and G have different values.
- C. C and F have the same value.
- D. D and E have the same value.

14. What is the output of the following program?

Pascal Version

```
var
  s:string = 'hkoi2013';
  c:char; i:longint;
begin
  c:='a';
  for i:=1 to 8 do
    if (s[i] > c) then
      begin
        write(s[i]);
        c:=s[i];
      end;
  end;
end.
```

C Version

```
#include <stdio.h>
char s[] = "hkoi2013";
char c = 'a'; int i;
int main() {
  for (i=0; i<8; ++i)
    if (s[i] > c) {
      printf("%c", s[i]);
      c = s[i];
    }
  return 0;
}
```

- A. hko
- B. hkoi
- C. hko23
- D. h20

15. Assume you know the following relationships:

- i. If it is cloudy today, Ken feels sad.
- ii. If Ken feels sad, he will play computer games for a whole day.
- iii. If Ken plays computer games for a whole day, he will eat a lot at dinner.

You know that Ken plays computer games for a whole day today, which of the following statements can be **TRUE**?

- A. Today is cloudy.
- B. Ken feels sad today.
- C. Ken eats a lot at dinner.
- D. All of above

16. Which of the following code segments will **NOT** exit?

Pascal Version

i.	a:=2013; while (a>0) inc(a);
ii.	b:=2013.0; while (b<>0.0) b:=b-0.5;
iii.	c:=2013.0; while (c<>0.0) c:=c-0.1;

C Version

i.	a=2013; while (a>0) ++a;
ii.	b=2013.0; while (b!=0.0) b=b-0.5;
iii.	c=2013.0; while (c!=0.0) c=c-0.1;

- A. i only
- B. ii only
- C. iii only
- D. ii and iii

For questions 17-19, consider the following program segment:

Pascal Version

```

procedure P1(n:longint);
var i,j,k:longint;
begin
  for i:=0 to n-1 do
    for j:=i+1 to n-1 do
      for k:=j+1 to n-1 do
        write('*');
end;
procedure P2(n:longint);
var i,j:longint;
begin
  for i:=0 to n-1 do
    for j:=0 to n-1 do
      write('*');
end;
procedure P3(n:longint);
var i:longint;
begin
  if (n >= 1) then
  begin
    for i:=0 to n-1 do
      write('*');
    P3(n div 2);
    P3(n div 2);
  end;
end;
procedure P4(n:longint);
begin
  if (n >= 5) then
  begin
    write('*');
    P4(n-1);
    P4(n-1);
  end;
end;
end;

```

C Version

```

void P1(int n){
  int i,j,k;
  for (i=0; i<n; i++)
    for (j=i+1; j<n; j++)
      for (k=j+1; k<n; k++)
        printf("*");
}
void P2(int n){
  int i,j;
  for (i=0; i<n; i++)
    for (j=0; j<n; j++)
      printf("*");
}
void P3(int n){
  int i;
  if (n >= 1){
    for (i=0; i<n; i++)
      printf("*");
    P3(n/2);
    P3(n/2);
  }
}
void P4(int n){
  if (n >= 5){
    printf("*");
    P4(n-1);
    P4(n-1);
  }
}

```

17. Among P1 (4), P2 (4), P3 (4) and P4 (4), which of them will print the most number of '*'?
- A. P1
 B. P2
 C. P3
 D. P4
18. Among P1 (9), P2 (9), P3 (9) and P4 (9), which of them prints the most number of '*'?
- A. P1
 B. P2
 C. P3
 D. P4
19. What is the minimum value of n such that P4 (n) prints more '*' than all P1 (n), P2 (n) and P3 (n)?
- A. 10
 B. 11
 C. 12
 D. Such n does not exist
20. What is the output of the following program?

Pascal Version

```
var s:string='hkoi2013';
    i:longint;
begin
  for i:=1 to 4 do
  begin
    s[i]:=s[9-i]; s[9-i]:=s[i];
  end;
  writeln(s);
end.
```

C Version

```
#include <stdio.h>
char s[] = "hkoi2013";
int i;
int main() {
  for (i=0; i<4; i++) {
    s[i] = s[7-i]; s[7-i] = s[i];
  }
  printf("%s\n",s);
}
```

- A. hkoi2013
 B. 3102iokh
 C. hkoiiokh
 D. 31022013

21. a, b, c are positive integers less than 10000 that represent the side lengths of a triangle.

Which of the following expressions **CANNOT** determine whether the triangle is valid?

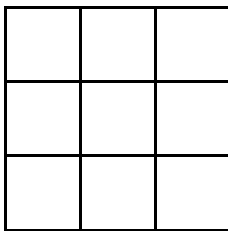
Pascal Version

- A. $(b > a - c) \text{ and } (a > c - b) \text{ and } (a + c > b)$
- B. $(a + b > c) \text{ and } (b + c > a) \text{ and } (c > b - a)$
- C. $(c > a - b) \text{ and } (a > b - c) \text{ and } (a > c - b)$
- D. $(c > b - a) \text{ and } (b > c - a) \text{ and } (a > b - c)$

C Version

- A. $(b > a - c) \ \&\& \ (a > c - b) \ \&\& \ (a + c > b)$
- B. $(a + b > c) \ \&\& \ (b + c > a) \ \&\& \ (c > b - a)$
- C. $(c > a - b) \ \&\& \ (a > b - c) \ \&\& \ (a > c - b)$
- D. $(c > b - a) \ \&\& \ (b > c - a) \ \&\& \ (a > b - c)$

22. How many ways are there to fill 2 cells with black such that the two black cells are **NOT** in the same row?



- A. 18
- B. 27
- C. 36
- D. 54

23. What is the output of the following program?

Pascal Version

```

var ans,i:longint;
function f(n:longint):longint;
var cnt,k:longint;
begin
  cnt:=0;
  k:=1;
  while (k<=n) do
  begin
    if (k and n > 0) then
      cnt:=cnt+1;
    k:=k*2;
  end;
  f:=cnt;
end;

begin
  ans:=0;
  for i:=0 to 15 do
    ans:=ans+f(i);
  writeln(ans);
end.
```

C Version

```

#include <stdio.h>
int ans, i;
int f(int n){
  int cnt,k;
  cnt=0;
  k=1;
  while (k<=n){
    if (k&n > 0)
      ++cnt;
    k*=2;
  }
  return cnt;
}

int main(){
  ans=0;
  for (i=0; i<16; i++)
    ans+=f(i);
  printf("%d\n",ans);
  return 0;
}
```


- A. 16
- B. 32
- C. 48
- D. 64

24. (Cancelled)

25. Consider the following function:

Pascal Version

```
function f(n:longint):longint;
var ans,i:longint;
begin
  ans:=n;
  for i:=2 to n do
  begin
    if (n mod i = 0) then
      ans:=ans div i*(i-1);
    while (n mod i = 0) do
      n:=n div i;
  end;
  f:=ans;
end;
```

C Version

```
int f(int n){
  int ans,i;
  ans=n;
  for (i=2; i<=n; i++){
    if (n%i==0)
      ans=ans/i*(i-1);
    while (n%i==0)
      n/=i;
  }
  return ans;
}
```

Which of the following input n produces the greatest value of $f(n)$?

- A. 53
- B. 54
- C. 55
- D. 56

END OF SECTION A

Section B (22 marks)

The blanks are labeled from A to K. Please fill in the blanks on the answer sheet.

Except otherwise specified, two marks for each correct blank. No marks will be deducted for wrong answers.

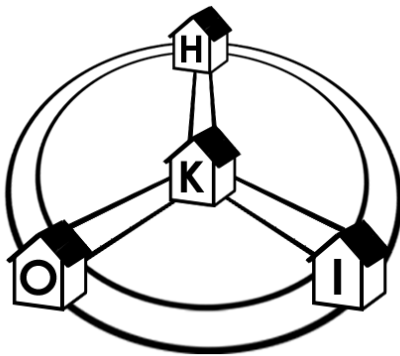
Note:

- (1) You must not use the ? : operator in C.
- (2) You must not use any library function unless the appropriate library(s) is/are included.
- (3) You can write only one character in each box on the answer sheet.
- (4) No answer with length greater than the designated number of boxes will be accepted.

1. Let x be the minimum positive multiple of 17 that contains only digit '1'. How many digits does x have?

_____ **A** _____

2.



The above figure shows a map of a village with 4 houses.

Houses and roads may be visited/used zero or more times.

Examples of paths of length 3 are $H \rightarrow K \rightarrow O \rightarrow I$ and $K \rightarrow I \rightarrow O \rightarrow I$.

Please note that $H \rightarrow K \rightarrow O \rightarrow I$, $H \rightarrow O \rightarrow K \rightarrow I$ and $I \rightarrow O \rightarrow K \rightarrow H$ are considered different.

The total number of different paths of length 3 is _____ **B** _____.

3. A rotation of a string is formed by removing zero or more consecutive characters from the left and append them to its right.

For example, $cdeab$ is a rotation of $abcde$.

Let $s = \text{"hkoi2013"}$, write a string q such that every rotation of s is a substring of q .

_____ **C** _____

4. Consider the following program:

Pascal Version

```

10 var
11   x1,y1,x2,y2:longint;
12 function dist(x1,y1,x2,y2:longint):longint;
13 begin
14   dist:=trunc(sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2)));
15 end;
16 begin
17   readln(x1,y1,x2,y2);
18   if (dist(x1,y1,x2,y2)<1) then
19     writeln('The distance is less than 1')
20   else if (dist(x1,y1,x2,y2)=1) then
21     writeln('The distance is 1')
22   else
23     writeln('The distance is greater than 1');
24 end.
```

C Version

```

50 #include <stdio.h>
51 #include <math.h>
52 int x1,y1,x2,y2;
53 int dist(int x1, int y1, int x2, int y2) {
54   return floor(sqrt((x1-x2)*(x1-x2)+(y1-y2)*(y1-y2)));
55 }
56 int main() {
57   scanf("%d %d %d %d",&x1,&y1,&x2,&y2);
58   if (dist(x1,y1,x2,y2)<1)
59     printf("The distance is less than 1\n");
60   else if (dist(x1,y1,x2,y2)==1)
61     printf("The distance is 1\n");
62   else
63     printf("The distance is greater than 1\n");
64   return 0;
65 }
```

The program checks if the distance between two coordinates (x_1, y_1) , (x_2, y_2) is less than, equal to, or greater than 1. You may assume that x_1, y_1, x_2 and y_2 are integers in $[-10000, 10000]$. Unfortunately, this program contains a logic error but it can be fixed by changing a single line. Identify the line and rewrite it.

Line Number: **D**

Rewrite the line: **E**

Note for C Version: `y1` is defined as `double y1(double)` in `<math.h>`.

In this question please assume that there is no such definition.

Disregard if you do not understand this note.

5. Assume array a (**Pascal**: $a[0..n-1]$, **C**: $a[n]$) consists of distinct positive integers and $\max(i, j)$ returns the maximum value between $a[i]$ to $a[j]$ inclusive.

Complete the program such that it finds the second maximum value of array a .

Pascal Version

```

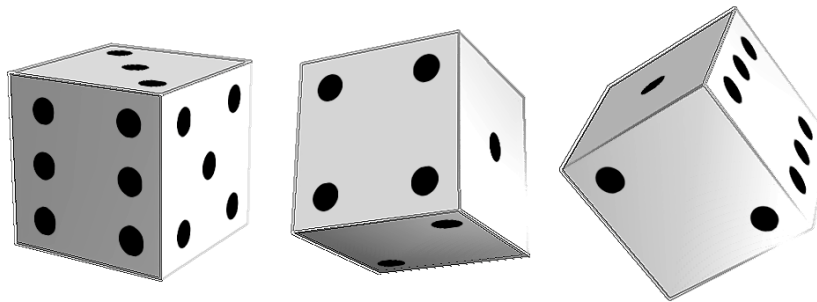
maximum := max(0, n-1);
for i:=0 to n-1 do
  if (_____ F _____) then
    _____ G _____;
a[i] := -a[i];
secondmaximum := _____ H _____;
a[i] := -a[i];
    
```

C Version

```

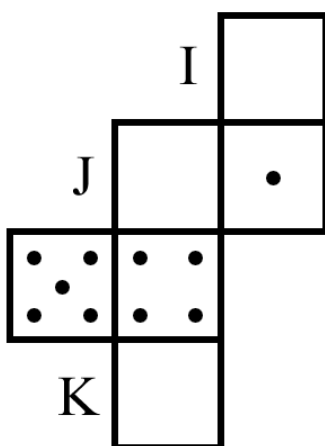
maximum = max(0, n-1);
for (i=0; i<n; i++)
  if (_____ F _____)
    _____ G _____;
a[i] = -a[i];
secondmaximum = _____ H _____;
a[i] = -a[i];
    
```

6. Observe the following non-standard die.



Now, complete its net on the answer sheet.

1 mark for each correct value. 2 marks for each correct value and orientation.



END OF PAPER